

COLLEGE ALGEBRA FUNCTION LIMITS

UNDERSTANDING COLLEGE ALGEBRA FUNCTION LIMITS

COLLEGE ALGEBRA FUNCTION LIMITS ARE A FOUNDATIONAL CONCEPT THAT UNLOCKS A DEEPER UNDERSTANDING OF CALCULUS AND ADVANCED MATHEMATICAL ANALYSIS. ESSENTIALLY, LIMITS DESCRIBE THE BEHAVIOR OF A FUNCTION AS ITS INPUT APPROACHES A PARTICULAR VALUE, WITHOUT NECESSARILY REACHING THAT VALUE. THIS IDEA OF "APPROACHING" IS CRUCIAL; IT ALLOWS US TO ANALYZE TRENDS, IDENTIFY ASYMPTOTES, AND PREDICT FUNCTION BEHAVIOR AT POINTS WHERE DIRECT SUBSTITUTION MIGHT LEAD TO UNDEFINED RESULTS. IN THIS COMPREHENSIVE EXPLORATION, WE'LL DELVE INTO THE DEFINITION OF LIMITS, VARIOUS TECHNIQUES FOR EVALUATING THEM, AND THEIR SIGNIFICANCE IN COLLEGE ALGEBRA. WE'LL COVER EVERYTHING FROM THE INTUITIVE CONCEPT OF GETTING "CLOSE" TO A VALUE TO THE FORMAL EPSILON-DELTA DEFINITION AND PRACTICAL APPLICATIONS. PREPARE TO DEMYSTIFY THE WORLD OF FUNCTION LIMITS AND BUILD A SOLID MATHEMATICAL TOOLKIT.

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WHAT IS A FUNCTION LIMIT?

AT ITS CORE, A FUNCTION LIMIT ANSWERS THE QUESTION: "WHAT VALUE DOES A FUNCTION'S OUTPUT GET CLOSER AND CLOSER TO AS ITS INPUT GETS CLOSER AND CLOSER TO A SPECIFIC NUMBER?" IT'S NOT ABOUT WHAT HAPPENS AT THE SPECIFIC NUMBER, BUT WHAT HAPPENS AROUND IT. THINK OF IT LIKE APPROACHING A DESTINATION ON A MAP; YOU'RE INTERESTED IN THE TOWN YOU'RE HEADING TOWARDS, NOT NECESSARILY THE EXACT SPOT WHERE THE ROAD ENDS. THIS CONCEPT IS FUNDAMENTAL BECAUSE MANY REAL-WORLD PHENOMENA, FROM VELOCITY TO POPULATION GROWTH, CAN BE MODELED BY FUNCTIONS, AND UNDERSTANDING THEIR LIMITING BEHAVIOR PROVIDES INVALUABLE INSIGHTS.

IN MATHEMATICAL NOTATION, WE EXPRESS A LIMIT AS: $\lim_{x \rightarrow c} f(x) = L$. THIS READS: "THE LIMIT OF FUNCTION $f(x)$ AS x APPROACHES c IS L ." HERE, c IS THE VALUE THAT THE INPUT x IS APPROACHING, AND L IS THE CORRESPONDING VALUE THAT THE OUTPUT $f(x)$ IS APPROACHING.

IT'S IMPORTANT TO DISTINGUISH BETWEEN THE LIMIT OF A FUNCTION AT A POINT AND THE ACTUAL VALUE OF THE FUNCTION AT THAT POINT. THE FUNCTION MIGHT BE UNDEFINED AT c , OR ITS VALUE AT c MIGHT BE DIFFERENT FROM THE LIMIT L . THE LIMIT IS SOLELY CONCERNED WITH THE TREND OF THE FUNCTION'S OUTPUTS AS THE INPUTS GET ARBITRARILY CLOSE TO c .

THE INTUITIVE APPROACH TO LIMITS

BEFORE DIVING INTO FORMAL DEFINITIONS AND CALCULATIONS, IT'S HELPFUL TO GRASP THE INTUITIVE IDEA OF A LIMIT. IMAGINE PLOTTING THE GRAPH OF A FUNCTION. AS YOU MOVE ALONG THE X-AXIS TOWARDS A SPECIFIC VALUE, SAY c , YOU OBSERVE THE CORRESPONDING Y-VALUES ON THE GRAPH. IF THESE Y-VALUES ARE CONSISTENTLY GETTING CLOSER AND CLOSER TO A PARTICULAR NUMBER, L , FROM BOTH SIDES (VALUES OF x LESS THAN c AND VALUES OF x GREATER THAN c), THEN WE SAY THE LIMIT OF THE FUNCTION AS x APPROACHES c IS L .

LET'S CONSIDER AN EXAMPLE: $f(x) = \frac{x^2 - 1}{x - 1}$. IF WE TRY TO FIND THE LIMIT AS x APPROACHES 1, DIRECT SUBSTITUTION $f(1)$ GIVES US $\frac{0}{0}$, WHICH IS AN INDETERMINATE FORM. HOWEVER, IF WE PICK VALUES OF x VERY CLOSE TO 1, LIKE 0.9, 0.99, 0.999, AND 1.1, 1.01, 1.001, WE'LL SEE THE FUNCTION'S OUTPUT GETTING CLOSER AND CLOSER TO 2.

THIS MEANS THAT EVEN THOUGH $f(1)$ IS UNDEFINED, THE LIMIT OF $f(x)$ AS x APPROACHES 1 IS 2. THE FUNCTION BEHAVES AS IF IT HAS A "HOLE" AT $x=1$, BUT THE VALUES AROUND THAT HOLE TEND TOWARDS 2.

METHODS FOR EVALUATING FUNCTION LIMITS

WHILE THE INTUITIVE APPROACH IS USEFUL FOR UNDERSTANDING, WE NEED SYSTEMATIC METHODS TO EVALUATE LIMITS ACCURATELY. SEVERAL TECHNIQUES ARE COMMONLY EMPLOYED IN COLLEGE ALGEBRA.

DIRECT SUBSTITUTION

THE SIMPLEST METHOD FOR EVALUATING A LIMIT IS DIRECT SUBSTITUTION. IF THE FUNCTION $f(x)$ IS CONTINUOUS AT $x=c$, MEANING IT'S DEFINED AT c AND THERE ARE NO BREAKS, JUMPS, OR HOLES IN ITS GRAPH AT THAT POINT, THEN THE LIMIT CAN BE FOUND BY SIMPLY PLUGGING c INTO THE FUNCTION: $\lim_{x \rightarrow c} f(x) = f(c)$.

THIS APPLIES TO MANY COMMON FUNCTIONS LIKE POLYNOMIALS, SINE, COSINE, AND EXPONENTIAL FUNCTIONS WITHIN THEIR DOMAINS. FOR INSTANCE, TO FIND $\lim_{x \rightarrow 2} (x^2 + 3x)$, WE CAN DIRECTLY SUBSTITUTE 2: $(2^2 + 3(2) = 4 + 6 = 10)$. THEREFORE, THE LIMIT IS 10.

FACTORING AND CANCELING

WHEN DIRECT SUBSTITUTION RESULTS IN AN INDETERMINATE FORM, SUCH AS $\frac{0}{0}$, FACTORING IS OFTEN THE NEXT STEP. THIS TECHNIQUE IS PARTICULARLY USEFUL FOR RATIONAL FUNCTIONS (RATIOS OF POLYNOMIALS). THE GOAL IS TO FACTOR BOTH THE NUMERATOR AND THE DENOMINATOR, IDENTIFY ANY COMMON FACTORS THAT ARE CAUSING THE INDETERMINATE FORM, AND CANCEL THEM OUT.

CONSIDER THE LIMIT $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$ AGAIN. WE CAN FACTOR THE NUMERATOR AS $((x-1)(x+1))$. SO, THE EXPRESSION BECOMES $\frac{(x-1)(x+1)}{x-1}$. FOR $(x \neq 1)$, WE CAN CANCEL THE $(x-1)$ TERMS, LEAVING US WITH $(x+1)$. NOW, WE CAN APPLY DIRECT SUBSTITUTION TO THE SIMPLIFIED EXPRESSION: $\lim_{x \rightarrow 1} (x+1) = 1+1 = 2$. THIS CONFIRMS OUR EARLIER INTUITIVE RESULT.

RATIONALIZING THE NUMERATOR OR DENOMINATOR

THIS METHOD IS EMPLOYED WHEN THE FUNCTION INVOLVES SQUARE ROOTS OR OTHER RADICALS, AND DIRECT SUBSTITUTION LEADS TO AN INDETERMINATE FORM. THE PROCESS INVOLVES MULTIPLYING THE NUMERATOR AND/OR DENOMINATOR BY THE CONJUGATE OF THE RADICAL EXPRESSION. THE CONJUGATE OF $(a + \sqrt{b})$ IS $(a - \sqrt{b})$, AND VICE VERSA. THIS MULTIPLICATION OFTEN HELPS TO ELIMINATE THE RADICAL FROM THE DENOMINATOR OR NUMERATOR, LEADING TO AN EXPRESSION THAT CAN BE SIMPLIFIED THROUGH FACTORING OR DIRECT SUBSTITUTION.

FOR EXAMPLE, TO EVALUATE $\lim_{x \rightarrow 0} \frac{\sqrt{x+1} - 1}{x}$, DIRECT SUBSTITUTION YIELDS $\frac{0}{0}$. WE MULTIPLY THE NUMERATOR AND DENOMINATOR BY THE CONJUGATE OF THE NUMERATOR, $(\sqrt{x+1} + 1)$:

$$\frac{(\sqrt{x+1} - 1)x}{x} \times \frac{(\sqrt{x+1} + 1)(\sqrt{x+1} + 1)}{(\sqrt{x+1} + 1)(\sqrt{x+1} + 1)} = \frac{((x+1) - 1)x}{x(\sqrt{x+1} + 1)} = \frac{x}{\sqrt{x+1} + 1}$$

CANCELING THE (x) TERM (SINCE $(x \neq 0)$ WHEN CONSIDERING THE LIMIT), WE GET $\frac{1}{\sqrt{x+1} + 1}$. NOW, DIRECT SUBSTITUTION OF $(x=0)$ GIVES $\frac{1}{\sqrt{0+1} + 1} = \frac{1}{1+1} = \frac{1}{2}$.

USING L'HÔPITAL'S RULE (FOR INDETERMINATE FORMS)

L'HÔPITAL'S RULE IS A POWERFUL TOOL FOR EVALUATING LIMITS OF INDETERMINATE FORMS LIKE $\frac{0}{0}$ OR $\frac{\infty}{\infty}$. IT STATES THAT IF $\lim_{x \rightarrow c} \frac{f(x)}{g(x)}$ RESULTS IN AN INDETERMINATE FORM, THEN THE LIMIT IS EQUAL TO THE LIMIT OF THE RATIO OF THEIR DERIVATIVES, PROVIDED THE LATTER LIMIT EXISTS. MATHEMATICALLY, $\lim_{x \rightarrow c} \frac{f(x)}{g(x)} = \lim_{x \rightarrow c} \frac{f'(x)}{g'(x)}$.

LET'S REVISIT $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$. THIS GIVES $\frac{0}{0}$. APPLYING L'HÔPITAL'S RULE, WE TAKE THE DERIVATIVE OF THE NUMERATOR $(2x)$ AND THE DERIVATIVE OF THE DENOMINATOR (1) . THE NEW LIMIT BECOMES $\lim_{x \rightarrow 1} \frac{2x}{1}$. DIRECT SUBSTITUTION YIELDS $\frac{2(1)}{1} = 2$. WHILE FACTORING IS OFTEN SIMPLER FOR POLYNOMIALS, L'HÔPITAL'S RULE IS INDISPENSABLE FOR MORE COMPLEX FUNCTIONS WHERE FACTORING IS DIFFICULT.

ONE-SIDED LIMITS

SOMETIMES, A FUNCTION MIGHT APPROACH DIFFERENT VALUES AS (x) APPROACHES (c) FROM THE LEFT (VALUES OF (x) LESS THAN (c)) COMPARED TO APPROACHING FROM THE RIGHT (VALUES OF (x) GREATER THAN (c)). THESE ARE CALLED ONE-SIDED LIMITS. THE LIMIT FROM THE LEFT IS DENOTED AS $\lim_{x \rightarrow c^-} f(x)$, AND THE LIMIT FROM THE RIGHT IS DENOTED AS $\lim_{x \rightarrow c^+} f(x)$.

FOR THE OVERALL LIMIT $\lim_{x \rightarrow c} f(x)$ TO EXIST, THE LEFT-SIDED LIMIT AND THE RIGHT-SIDED LIMIT MUST BE EQUAL. THAT IS, $\lim_{x \rightarrow c} f(x) = L$ IF AND ONLY IF $\lim_{x \rightarrow c^-} f(x) = L$ AND $\lim_{x \rightarrow c^+} f(x) = L$. THIS CONCEPT IS PARTICULARLY IMPORTANT WHEN DEALING WITH PIECEWISE FUNCTIONS OR FUNCTIONS WITH SHARP CORNERS OR JUMPS.

FOR INSTANCE, CONSIDER THE FUNCTION $(f(x) = |x|/x)$. AS (x) APPROACHES 0 FROM THE RIGHT $(x > 0)$, $(|x|=x)$, SO $(f(x) = x/x = 1)$. THUS, $\lim_{x \rightarrow 0^+} \frac{|x|}{x} = 1$. HOWEVER, AS (x) APPROACHES 0 FROM THE LEFT $(x < 0)$, $(|x|=-x)$, SO $(f(x) = -x/x = -1)$. THUS, $\lim_{x \rightarrow 0^-} \frac{|x|}{x} = -1$. SINCE THE ONE-

SIDED LIMITS ARE NOT EQUAL, THE OVERALL LIMIT $\lim_{x \rightarrow 0} \frac{|x|}{x}$ DOES NOT EXIST.

LIMITS AT INFINITY

LIMITS AT INFINITY EXPLORE THE BEHAVIOR OF A FUNCTION AS ITS INPUT x GROWS INFINITELY LARGE (POSITIVE OR NEGATIVE). WE WRITE THIS AS $\lim_{x \rightarrow \infty} f(x)$ OR $\lim_{x \rightarrow -\infty} f(x)$. THESE LIMITS HELP US UNDERSTAND THE END BEHAVIOR OF A FUNCTION AND IDENTIFY HORIZONTAL ASYMPTOTES.

FOR RATIONAL FUNCTIONS, THE LIMIT AT INFINITY OFTEN DEPENDS ON THE DEGREES OF THE NUMERATOR AND DENOMINATOR. IF THE DEGREE OF THE NUMERATOR IS LESS THAN THE DEGREE OF THE DENOMINATOR, THE LIMIT IS 0. IF THE DEGREES ARE EQUAL, THE LIMIT IS THE RATIO OF THE LEADING COEFFICIENTS. IF THE DEGREE OF THE NUMERATOR IS GREATER THAN THE DEGREE OF THE DENOMINATOR, THE LIMIT IS EITHER ∞ OR $-\infty$, DEPENDING ON THE SIGNS OF THE LEADING COEFFICIENTS.

FOR EXAMPLE, $\lim_{x \rightarrow \infty} \frac{3x^2 + 1}{x^2 - 4}$. SINCE THE DEGREES OF THE NUMERATOR AND DENOMINATOR ARE BOTH 2, THE LIMIT IS THE RATIO OF THE LEADING COEFFICIENTS, WHICH IS $\frac{3}{1} = 3$. THIS INDICATES A HORIZONTAL ASYMPTOTE AT $y=3$.

INFINITE LIMITS

INFINITE LIMITS DESCRIBE SITUATIONS WHERE THE FUNCTION'S OUTPUT GROWS WITHOUT BOUND (EITHER POSITIVELY OR NEGATIVELY) AS THE INPUT APPROACHES A SPECIFIC VALUE. THIS OFTEN OCCURS WHEN A FUNCTION HAS A VERTICAL ASYMPTOTE. WE DENOTE AN INFINITE LIMIT AS $\lim_{x \rightarrow c} f(x) = \infty$ OR $\lim_{x \rightarrow c} f(x) = -\infty$.

CONSIDER THE FUNCTION $f(x) = \frac{1}{(x-2)^2}$. AS x APPROACHES 2 FROM EITHER THE LEFT OR THE RIGHT, THE DENOMINATOR $(x-2)^2$ GETS VERY CLOSE TO 0 BUT REMAINS POSITIVE. THIS CAUSES THE FRACTION TO BECOME VERY LARGE AND POSITIVE. THEREFORE, $\lim_{x \rightarrow 2} \frac{1}{(x-2)^2} = \infty$. THIS SIGNIFIES A VERTICAL ASYMPTOTE AT $x=2$.

UNDERSTANDING INFINITE LIMITS IS CRUCIAL FOR IDENTIFYING ASYMPTOTES, WHICH ARE ESSENTIAL FEATURES IN SKETCHING AND ANALYZING THE GRAPHS OF FUNCTIONS.

CONTINUITY AND LIMITS

THE CONCEPT OF LIMITS IS INTRINSICALLY LINKED TO CONTINUITY. A FUNCTION $f(x)$ IS CONSIDERED CONTINUOUS AT A POINT $x=c$ IF THREE CONDITIONS ARE MET:

- $f(c)$ IS DEFINED.
- $\lim_{x \rightarrow c} f(x)$ EXISTS.
- $\lim_{x \rightarrow c} f(x) = f(c)$.

IN SIMPLER TERMS, A FUNCTION IS CONTINUOUS AT A POINT IF YOU CAN DRAW ITS GRAPH THROUGH THAT POINT WITHOUT LIFTING YOUR PEN. IF ANY OF THESE CONDITIONS ARE VIOLATED, THE FUNCTION HAS A DISCONTINUITY AT THAT POINT.

TYPES OF DISCONTINUITIES INCLUDE REMOVABLE DISCONTINUITIES (HOLES), JUMP DISCONTINUITIES, AND INFINITE DISCONTINUITIES (VERTICAL ASYMPTOTES). UNDERSTANDING LIMITS ALLOWS US TO PRECISELY IDENTIFY AND CLASSIFY THESE

DISCONTINUITIES, WHICH IS VITAL FOR A THOROUGH ANALYSIS OF FUNCTION BEHAVIOR.

WHY ARE FUNCTION LIMITS IMPORTANT IN COLLEGE ALGEBRA?

FUNCTION LIMITS SERVE AS THE BEDROCK FOR MANY ADVANCED MATHEMATICAL CONCEPTS ENCOUNTERED IN COLLEGE ALGEBRA AND BEYOND. THEY ARE NOT MERELY ABSTRACT THEORETICAL CONSTRUCTS BUT PRACTICAL TOOLS THAT ENABLE US TO SOLVE COMPLEX PROBLEMS AND UNDERSTAND INTRICATE PHENOMENA.

- **FOUNDATION FOR CALCULUS:** LIMITS ARE THE DEFINING CONCEPT OF CALCULUS. DERIVATIVES, WHICH MEASURE RATES OF CHANGE, ARE DEFINED AS LIMITS OF DIFFERENCE QUOTIENTS. INTEGRALS, WHICH REPRESENT AREAS UNDER CURVES, ARE DEFINED AS LIMITS OF RIEMANN SUMS. WITHOUT A FIRM GRASP OF LIMITS, UNDERSTANDING CALCULUS IS IMPOSSIBLE.
- **UNDERSTANDING FUNCTION BEHAVIOR:** LIMITS HELP US UNDERSTAND HOW FUNCTIONS BEHAVE AT POINTS WHERE THEY MIGHT BE UNDEFINED OR AT EXTREME VALUES. THIS IS CRUCIAL FOR ANALYZING ASYMPTOTES, IDENTIFYING TRENDS, AND PREDICTING FUTURE BEHAVIOR IN MODELS.
- **ANALYZING RATES OF CHANGE:** IN REAL-WORLD APPLICATIONS, WE ARE OFTEN INTERESTED IN HOW QUANTITIES CHANGE OVER TIME. LIMITS PROVIDE THE MATHEMATICAL FRAMEWORK FOR PRECISELY DEFINING AND CALCULATING INSTANTANEOUS RATES OF CHANGE, WHICH ARE FUNDAMENTAL TO PHYSICS, ENGINEERING, ECONOMICS, AND MANY OTHER FIELDS.
- **SOLVING INDETERMINATE FORMS:** MANY PROBLEMS IN MATHEMATICS AND SCIENCE LEAD TO INDETERMINATE FORMS WHEN DIRECT SUBSTITUTION IS ATTEMPTED. LIMIT TECHNIQUES, SUCH AS FACTORING, RATIONALIZING, AND L'HÔPITAL'S RULE, PROVIDE SYSTEMATIC WAYS TO RESOLVE THESE INDETERMINACIES AND FIND MEANINGFUL SOLUTIONS.
- **DEFINING CONTINUITY:** THE RIGOROUS DEFINITION OF CONTINUITY RELIES ON THE EXISTENCE OF LIMITS. UNDERSTANDING CONTINUITY IS ESSENTIAL FOR WORKING WITH FUNCTIONS, ESPECIALLY IN AREAS LIKE ANALYSIS AND TOPOLOGY, AND FOR ENSURING THAT MATHEMATICAL MODELS ACCURATELY REPRESENT CONTINUOUS PROCESSES.

MASTERING FUNCTION LIMITS IN COLLEGE ALGEBRA IS AN INVESTMENT THAT PAYS DIVIDENDS THROUGHOUT YOUR MATHEMATICAL JOURNEY. IT EQUIPS YOU WITH THE ANALYTICAL POWER TO TACKLE INCREASINGLY COMPLEX IDEAS AND UNLOCK A DEEPER APPRECIATION FOR THE ELEGANCE AND UTILITY OF MATHEMATICS.

FAQ: COLLEGE ALGEBRA FUNCTION LIMITS

Q: WHAT DOES IT MEAN FOR A FUNCTION TO HAVE A LIMIT AT A CERTAIN POINT?

A: IT MEANS THAT AS THE INPUT VALUES OF THE FUNCTION GET ARBITRARILY CLOSE TO A SPECIFIC NUMBER, THE OUTPUT VALUES OF THE FUNCTION GET ARBITRARILY CLOSE TO A PARTICULAR VALUE, REGARDLESS OF WHETHER THE FUNCTION IS ACTUALLY DEFINED AT THAT SPECIFIC INPUT NUMBER.

Q: CAN A FUNCTION HAVE A LIMIT AT A POINT WHERE IT IS NOT DEFINED?

A: YES, ABSOLUTELY. THIS IS A CORE CONCEPT OF LIMITS. FOR EXAMPLE, THE FUNCTION $f(x) = \frac{x^2 - 4}{x - 2}$ IS NOT DEFINED AT $x = 2$, BUT ITS LIMIT AS x APPROACHES 2 IS 4 BECAUSE THE FUNCTION'S VALUES GET VERY CLOSE TO 4 AS x GETS CLOSE TO 2.

Q: HOW IS A ONE-SIDED LIMIT DIFFERENT FROM A REGULAR LIMIT?

A: A ONE-SIDED LIMIT EXAMINES THE BEHAVIOR OF A FUNCTION AS THE INPUT APPROACHES A VALUE FROM ONLY ONE DIRECTION (EITHER FROM THE LEFT OR FROM THE RIGHT). A REGULAR LIMIT REQUIRES THE FUNCTION TO APPROACH THE SAME VALUE FROM BOTH THE LEFT AND THE RIGHT.

Q: WHEN WOULD I USE L'HÔPITAL'S RULE TO EVALUATE A LIMIT?

A: YOU WOULD USE L'HÔPITAL'S RULE WHEN DIRECT SUBSTITUTION INTO THE LIMIT EXPRESSION RESULTS IN AN INDETERMINATE FORM, SPECIFICALLY $\frac{0}{0}$ OR $\frac{\infty}{\infty}$. IT INVOLVES TAKING THE DERIVATIVES OF THE NUMERATOR AND DENOMINATOR SEPARATELY.

Q: WHAT IS THE SIGNIFICANCE OF LIMITS AT INFINITY IN COLLEGE ALGEBRA?

A: LIMITS AT INFINITY HELP US UNDERSTAND THE END BEHAVIOR OF A FUNCTION – WHAT HAPPENS TO THE OUTPUT AS THE INPUT GROWS EXTREMELY LARGE (POSITIVE OR NEGATIVE). THIS IS CRUCIAL FOR IDENTIFYING HORIZONTAL ASYMPTOTES.

Q: HOW DO LIMITS RELATE TO THE CONCEPT OF CONTINUITY?

A: A FUNCTION IS CONTINUOUS AT A POINT IF THE LIMIT OF THE FUNCTION EXISTS AT THAT POINT, THE FUNCTION IS DEFINED AT THAT POINT, AND THE VALUE OF THE LIMIT IS EQUAL TO THE VALUE OF THE FUNCTION AT THAT POINT. LIMITS ARE THE FOUNDATION FOR DEFINING CONTINUITY.

Q: WHAT HAPPENS IF THE LEFT-SIDED LIMIT AND THE RIGHT-SIDED LIMIT ARE DIFFERENT?

A: IF THE LEFT-SIDED LIMIT AND THE RIGHT-SIDED LIMIT AT A POINT ARE DIFFERENT, THEN THE OVERALL LIMIT OF THE FUNCTION AT THAT POINT DOES NOT EXIST.

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