

CHI SQUARED TEST EXPLAINED

THE CHI SQUARED TEST EXPLAINED: A COMPREHENSIVE GUIDE TO UNDERSTANDING THIS POWERFUL STATISTICAL TOOL

CHI SQUARED TEST EXPLAINED IN SIMPLE TERMS IS A STATISTICAL HYPOTHESIS TEST THAT DETERMINES WHETHER THERE IS A SIGNIFICANT ASSOCIATION BETWEEN TWO CATEGORICAL VARIABLES. IT'S A CORNERSTONE OF INFERENCE STATISTICS, ENABLING RESEARCHERS AND DATA ANALYSTS TO DRAW MEANINGFUL CONCLUSIONS FROM OBSERVED FREQUENCIES COMPARED TO EXPECTED FREQUENCIES. THIS POWERFUL TOOL HELPS US UNDERSTAND IF OBSERVED PATTERNS IN DATA ARE LIKELY DUE TO RANDOM CHANCE OR IF THEY REPRESENT A GENUINE RELATIONSHIP. WHETHER YOU'RE ANALYZING SURVEY RESULTS, MEDICAL OUTCOMES, OR MARKETING CAMPAIGN PERFORMANCE, GRASPING THE CHI-SQUARED TEST WILL SIGNIFICANTLY ENHANCE YOUR DATA INTERPRETATION CAPABILITIES. THIS ARTICLE WILL DELVE INTO ITS CORE CONCEPTS, OUTLINE ITS DIFFERENT TYPES, GUIDE YOU THROUGH THE CALCULATION PROCESS, AND DISCUSS ITS APPLICATIONS AND LIMITATIONS.

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WHAT IS A CHI SQUARED TEST?

THE CHI-SQUARED (χ^2) TEST IS A NON-PARAMETRIC STATISTICAL TEST USED TO ANALYZE CATEGORICAL DATA. IT IS PARTICULARLY USEFUL WHEN YOU WANT TO DETERMINE IF THERE IS A SIGNIFICANT DIFFERENCE BETWEEN AN OBSERVED FREQUENCY DISTRIBUTION AND AN EXPECTED FREQUENCY DISTRIBUTION. IN ESSENCE, IT QUANTIZES THE DIFFERENCE BETWEEN WHAT YOU SEE IN YOUR DATA AND WHAT YOU WOULD EXPECT TO SEE IF THERE WERE NO RELATIONSHIP BETWEEN THE VARIABLES UNDER CONSIDERATION. THIS TEST IS WIDELY APPLICABLE ACROSS VARIOUS FIELDS, FROM SOCIAL SCIENCES TO BIOLOGY, PROVIDING A ROBUST METHOD FOR HYPOTHESIS TESTING WHEN DEALING WITH COUNTS OR PROPORTIONS.

AT ITS HEART, THE CHI-SQUARED TEST ADDRESSES THE QUESTION OF WHETHER OBSERVED DIFFERENCES IN PROPORTIONS OR FREQUENCIES ARE STATISTICALLY SIGNIFICANT OR MERELY THE RESULT OF RANDOM VARIATION. IT ACHIEVES THIS BY CALCULATING A STATISTIC THAT MEASURES THE DISCREPANCY BETWEEN THE OBSERVED COUNTS IN YOUR DATA AND THE COUNTS YOU WOULD EXPECT UNDER A NULL HYPOTHESIS OF NO ASSOCIATION OR NO DIFFERENCE. UNDERSTANDING THIS FUNDAMENTAL CONCEPT IS CRUCIAL FOR APPLYING THE TEST CORRECTLY AND INTERPRETING ITS OUTCOMES WITH CONFIDENCE.

THE UNDERLYING PRINCIPLE: OBSERVED VS. EXPECTED FREQUENCIES

THE CORE PRINCIPLE DRIVING THE CHI-SQUARED TEST IS THE COMPARISON BETWEEN OBSERVED FREQUENCIES AND EXPECTED

FREQUENCIES. OBSERVED FREQUENCIES ARE THE ACTUAL COUNTS YOU COLLECT IN YOUR SAMPLE DATA. FOR EXAMPLE, IF YOU SURVEY 100 PEOPLE AND FIND 60 PREFER BRAND A AND 40 PREFER BRAND B, THESE ARE YOUR OBSERVED FREQUENCIES.

EXPECTED FREQUENCIES, ON THE OTHER HAND, REPRESENT THE COUNTS YOU WOULD ANTICIPATE IF A SPECIFIC NULL HYPOTHESIS WERE TRUE. THIS NULL HYPOTHESIS OFTEN POSITS THAT THERE IS NO RELATIONSHIP BETWEEN THE VARIABLES BEING STUDIED. FOR INSTANCE, IF YOU HYPOTHESIZE THAT BRAND PREFERENCE IS EVENLY SPLIT (50/50), YOUR EXPECTED FREQUENCIES FOR 100 PEOPLE WOULD BE 50 FOR BRAND A AND 50 FOR BRAND B. THE CHI-SQUARED TEST QUANTIFIES HOW MUCH THE OBSERVED FREQUENCIES DEVIATE FROM THESE EXPECTED FREQUENCIES.

THE GREATER THE DIFFERENCE BETWEEN THE OBSERVED AND EXPECTED FREQUENCIES, THE LARGER THE CHI-SQUARED STATISTIC WILL BE. THIS LARGER STATISTIC, IN TURN, SUGGESTS THAT THE OBSERVED DIFFERENCES ARE LESS LIKELY TO BE DUE TO RANDOM CHANCE AND MORE LIKELY TO INDICATE A GENUINE RELATIONSHIP OR EFFECT.

TYPES OF CHI SQUARED TESTS

THERE ARE SEVERAL VARIATIONS OF THE CHI-SQUARED TEST, EACH DESIGNED FOR SPECIFIC RESEARCH QUESTIONS AND DATA STRUCTURES. THE MOST COMMON TYPES ARE THE GOODNESS-OF-FIT TEST AND THE TEST FOR INDEPENDENCE (AND ITS CLOSE COUSIN, THE TEST FOR HOMOGENEITY).

CHI SQUARED GOODNESS-OF-FIT TEST

THE CHI-SQUARED GOODNESS-OF-FIT TEST IS USED TO DETERMINE WHETHER A SAMPLE DISTRIBUTION MATCHES A KNOWN OR HYPOTHESIZED POPULATION DISTRIBUTION. IT'S APPLIED WHEN YOU HAVE ONE CATEGORICAL VARIABLE AND YOU WANT TO SEE IF THE OBSERVED PROPORTIONS IN YOUR SAMPLE ALIGN WITH EXPECTED PROPORTIONS DERIVED FROM A THEORY OR A KNOWN DISTRIBUTION.

FOR EXAMPLE, IF A COMPANY CLAIMS ITS PRODUCT COMES IN FIVE COLORS WITH EQUAL PROBABILITY, A GOODNESS-OF-FIT TEST CAN BE USED TO SEE IF THE OBSERVED COUNTS OF EACH COLOR SOLD IN A SAMPLE OF SALES DATA MATCH THIS EXPECTED EQUAL DISTRIBUTION. IF THE OBSERVED COUNTS SIGNIFICANTLY DEVIATE FROM THE EXPECTED EQUAL COUNTS, YOU WOULD REJECT THE HYPOTHESIS THAT THE COLORS ARE EQUALLY PROBABLE.

CHI SQUARED TEST FOR INDEPENDENCE

THE CHI-SQUARED TEST FOR INDEPENDENCE IS THE MOST FREQUENTLY ENCOUNTERED TYPE. IT IS USED TO DETERMINE WHETHER THERE IS A STATISTICALLY SIGNIFICANT ASSOCIATION BETWEEN TWO CATEGORICAL VARIABLES IN A SINGLE POPULATION. THIS TEST HELPS ASCERTAIN IF THE TWO VARIABLES ARE INDEPENDENT OF EACH OTHER.

CONSIDER A STUDY INVESTIGATING WHETHER THERE IS A RELATIONSHIP BETWEEN SMOKING STATUS (SMOKER/NON-SMOKER) AND THE INCIDENCE OF LUNG CANCER (YES/NO). A CHI-SQUARED TEST FOR INDEPENDENCE WOULD ANALYZE A CONTINGENCY TABLE OF THESE TWO VARIABLES TO SEE IF SMOKING IS INDEPENDENT OF DEVELOPING LUNG CANCER OR IF THERE IS A SIGNIFICANT ASSOCIATION.

CHI SQUARED TEST FOR HOMOGENEITY

THE CHI-SQUARED TEST FOR HOMOGENEITY IS USED TO COMPARE THE DISTRIBUTION OF A CATEGORICAL VARIABLE ACROSS TWO OR MORE DISTINCT POPULATIONS. IT ADDRESSES WHETHER THE PROPORTIONS OF A CERTAIN CHARACTERISTIC ARE THE SAME ACROSS DIFFERENT GROUPS. WHILE MATHEMATICALLY SIMILAR TO THE TEST FOR INDEPENDENCE, THE RESEARCH QUESTION

AND STUDY DESIGN ARE DIFFERENT.

FOR INSTANCE, IF YOU WANT TO COMPARE THE PREFERENCE FOR A NEW SMARTPHONE FEATURE (LIKE/DISLIKE) BETWEEN USERS IN THREE DIFFERENT AGE GROUPS (E.G., GEN Z, MILLENNIALS, GEN X), YOU WOULD USE A TEST FOR HOMOGENEITY. YOU ARE CHECKING IF THE PREFERENCE DISTRIBUTION FOR THE FEATURE IS HOMOGENEOUS ACROSS THESE AGE DEMOGRAPHICS.

HOW TO PERFORM A CHI SQUARED TEST

PERFORMING A CHI-SQUARED TEST INVOLVES A SYSTEMATIC, STEP-BY-STEP PROCESS. WHILE STATISTICAL SOFTWARE AUTOMATES THESE CALCULATIONS, UNDERSTANDING THE UNDERLYING STEPS IS CRUCIAL FOR INTERPRETATION.

STEP 1: FORMULATE THE HYPOTHESES

EVERY STATISTICAL TEST BEGINS WITH DEFINING THE NULL HYPOTHESIS (H_0) AND THE ALTERNATIVE HYPOTHESIS (H_1). FOR A CHI-SQUARED TEST:

- THE NULL HYPOTHESIS (H_0) TYPICALLY STATES THAT THERE IS NO ASSOCIATION BETWEEN THE CATEGORICAL VARIABLES (FOR INDEPENDENCE/HOMOGENEITY) OR THAT THE OBSERVED DISTRIBUTION MATCHES THE EXPECTED DISTRIBUTION (FOR GOODNESS-OF-FIT).
- THE ALTERNATIVE HYPOTHESIS (H_1) STATES THAT THERE IS AN ASSOCIATION BETWEEN THE CATEGORICAL VARIABLES OR THAT THE OBSERVED DISTRIBUTION DOES NOT MATCH THE EXPECTED DISTRIBUTION.

STEP 2: CONSTRUCT THE CONTINGENCY TABLE

A CONTINGENCY TABLE (ALSO KNOWN AS A CROSS-TABULATION OR CROSSTAB) IS A TABLE THAT DISPLAYS THE FREQUENCY DISTRIBUTION OF TWO OR MORE CATEGORICAL VARIABLES. THE ROWS REPRESENT THE CATEGORIES OF ONE VARIABLE, AND THE COLUMNS REPRESENT THE CATEGORIES OF ANOTHER. THE CELLS WITHIN THE TABLE CONTAIN THE OBSERVED COUNTS FOR EACH COMBINATION OF CATEGORIES.

FOR EXAMPLE, FOR THE SMOKING AND LUNG CANCER STUDY:

	Lung Cancer: Yes	Lung Cancer: No
Smoker	Observed Count 1	Observed Count 2
Non-Smoker	Observed Count 3	Observed Count 4

STEP 3: CALCULATE EXPECTED FREQUENCIES

UNDER THE ASSUMPTION THAT THE NULL HYPOTHESIS IS TRUE, YOU CALCULATE THE EXPECTED FREQUENCIES FOR EACH CELL IN THE CONTINGENCY TABLE. THE FORMULA FOR EXPECTED FREQUENCY (E) IS:

$E = (\text{Row Total} \times \text{Column Total}) / \text{Grand Total}$

YOU WOULD CALCULATE THIS FOR EVERY CELL. FOR INSTANCE, THE EXPECTED COUNT FOR 'SMOKER' AND 'LUNG CANCER: YES' WOULD BE THE SUM OF ALL SMOKERS MULTIPLIED BY THE SUM OF ALL LUNG CANCER CASES, DIVIDED BY THE TOTAL NUMBER OF INDIVIDUALS IN THE STUDY.

STEP 4: CALCULATE THE CHI SQUARED STATISTIC

THE CHI-SQUARED STATISTIC (χ^2) IS CALCULATED BY SUMMING THE SQUARED DIFFERENCES BETWEEN OBSERVED (O) AND EXPECTED (E) FREQUENCIES, DIVIDED BY THE EXPECTED FREQUENCIES, ACROSS ALL CELLS:

$$\chi^2 = \sum [(O - E)^2 / E]$$

THIS FORMULA QUANTIFIES THE OVERALL DISCREPANCY BETWEEN WHAT WAS OBSERVED AND WHAT WAS EXPECTED UNDER THE NULL HYPOTHESIS. A LARGER χ^2 VALUE INDICATES A GREATER DIVERGENCE.

STEP 5: DETERMINE DEGREES OF FREEDOM

DEGREES OF FREEDOM (DF) ARE CRUCIAL FOR DETERMINING THE APPROPRIATE CHI-SQUARED DISTRIBUTION TO USE FOR STATISTICAL INFERENCE. THE DEGREES OF FREEDOM REPRESENT THE NUMBER OF VALUES IN THE CALCULATION THAT ARE FREE TO VARY.

- FOR A CHI-SQUARED GOODNESS-OF-FIT TEST WITH 'K' CATEGORIES, $DF = k - 1$.
- FOR A CHI-SQUARED TEST OF INDEPENDENCE OR HOMOGENEITY WITH 'R' ROWS AND 'C' COLUMNS, $DF = (R - 1) \times (C - 1)$.

STEP 6: FIND THE P-VALUE

THE P-VALUE REPRESENTS THE PROBABILITY OF OBSERVING A CHI-SQUARED STATISTIC AS EXTREME AS, OR MORE EXTREME THAN, THE ONE CALCULATED, ASSUMING THE NULL HYPOTHESIS IS TRUE. YOU CAN FIND THE P-VALUE USING A CHI-SQUARED DISTRIBUTION TABLE OR STATISTICAL SOFTWARE, GIVEN YOUR CALCULATED χ^2 STATISTIC AND DEGREES OF FREEDOM.

STEP 7: MAKE A DECISION

YOU COMPARE YOUR P-VALUE TO A PREDETERMINED SIGNIFICANCE LEVEL (α), WHICH IS COMMONLY SET AT 0.05.

- IF $P\text{-VALUE} \leq \alpha$: YOU REJECT THE NULL HYPOTHESIS (H_0). THIS SUGGESTS THAT THERE IS A STATISTICALLY SIGNIFICANT ASSOCIATION BETWEEN THE VARIABLES OR THAT THE OBSERVED DISTRIBUTION IS SIGNIFICANTLY DIFFERENT FROM THE EXPECTED DISTRIBUTION.
- IF $P\text{-VALUE} > \alpha$: YOU FAIL TO REJECT THE NULL HYPOTHESIS (H_0). THIS MEANS THERE IS NOT ENOUGH EVIDENCE TO CONCLUDE A STATISTICALLY SIGNIFICANT ASSOCIATION OR DIFFERENCE; THE OBSERVED DIFFERENCES COULD REASONABLY BE DUE TO RANDOM CHANCE.

INTERPRETING THE CHI SQUARED RESULTS

THE INTERPRETATION OF CHI-SQUARED TEST RESULTS HINGES ON THE P-VALUE AND THE EFFECT SIZE (THOUGH EFFECT SIZE ISN'T DIRECTLY CALCULATED BY THE STANDARD CHI-SQUARED FORMULA ITSELF, IT CAN BE INFERRED OR CALCULATED WITH ADDITIONAL MEASURES). A STATISTICALLY SIGNIFICANT RESULT (LOW P-VALUE) INDICATES THAT THE OBSERVED PATTERN IS UNLIKELY TO HAVE OCCURRED BY CHANCE ALONE, SUPPORTING THE ALTERNATIVE HYPOTHESIS.

HOWEVER, A SIGNIFICANT CHI-SQUARED STATISTIC DOES NOT TELL YOU THE DIRECTION OR STRENGTH OF THE ASSOCIATION. FOR INSTANCE, IN A TEST OF INDEPENDENCE, A SIGNIFICANT RESULT MEANS THE VARIABLES ARE RELATED, BUT IT DOESN'T EXPLAIN HOW THEY ARE RELATED (E.G., IS SMOKING MORE LIKELY TO LEAD TO LUNG CANCER, OR LESS LIKELY?). EXAMINING THE OBSERVED AND EXPECTED FREQUENCIES WITHIN THE CONTINGENCY TABLE, OR CALCULATING MEASURES LIKE CRAMER'S V FOR ASSOCIATION STRENGTH, IS CRUCIAL FOR A COMPLETE UNDERSTANDING.

CONVERSELY, FAILING TO REJECT THE NULL HYPOTHESIS DOESN'T PROVE THAT THERE'S NO RELATIONSHIP; IT SIMPLY MEANS THE DATA DID NOT PROVIDE SUFFICIENT EVIDENCE TO DETECT ONE AT YOUR CHOSEN SIGNIFICANCE LEVEL. SMALL SAMPLE SIZES OR WEAK ASSOCIATIONS CAN LEAD TO NON-SIGNIFICANT RESULTS EVEN WHEN A REAL EFFECT EXISTS.

ASSUMPTIONS OF THE CHI SQUARED TEST

FOR THE RESULTS OF A CHI-SQUARED TEST TO BE VALID, SEVERAL ASSUMPTIONS MUST BE MET:

- **CATEGORICAL DATA:** THE VARIABLES UNDER ANALYSIS MUST BE NOMINAL OR ORDINAL CATEGORICAL VARIABLES.
- **INDEPENDENCE OF OBSERVATIONS:** EACH OBSERVATION IN THE DATASET MUST BE INDEPENDENT OF ALL OTHER OBSERVATIONS. THIS MEANS THAT THE OUTCOME FOR ONE INDIVIDUAL SHOULD NOT INFLUENCE THE OUTCOME FOR ANOTHER.
- **RANDOM SAMPLING:** THE DATA SHOULD IDEALLY BE COLLECTED FROM A RANDOM SAMPLE OF THE POPULATION OF INTEREST.
- **SUFFICIENT SAMPLE SIZE:** EACH EXPECTED CELL FREQUENCY SHOULD BE SUFFICIENTLY LARGE. A COMMON RULE OF THUMB IS THAT AT LEAST 80% OF EXPECTED CELL FREQUENCIES SHOULD BE 5 OR GREATER, AND NO EXPECTED CELL FREQUENCY SHOULD BE LESS THAN 1. IF THIS ASSUMPTION IS VIOLATED, ALTERNATIVE TESTS LIKE FISHER'S EXACT TEST MIGHT BE MORE APPROPRIATE FOR SMALL 2x2 TABLES, OR ADJUSTMENTS MIGHT BE NEEDED FOR LARGER TABLES.

REAL-WORLD APPLICATIONS OF THE CHI SQUARED TEST

THE CHI-SQUARED TEST IS A VERSATILE TOOL WITH APPLICATIONS SPANNING NUMEROUS DISCIPLINES:

- **MARKET RESEARCH:** ANALYZING WHETHER CUSTOMER PREFERENCES FOR PRODUCT FEATURES ARE INDEPENDENT OF DEMOGRAPHIC GROUPS (AGE, GENDER, INCOME).
- **MEDICINE AND PUBLIC HEALTH:** INVESTIGATING ASSOCIATIONS BETWEEN RISK FACTORS (E.G., DIET, EXERCISE HABITS) AND DISEASE OUTCOMES (E.G., HEART DISEASE, DIABETES).
- **GENETICS:** TESTING WHETHER OBSERVED RATIOS OF OFFSPRING PHENOTYPES (PHYSICAL TRAITS) CONFORM TO MENDELIAN INHERITANCE PATTERNS.
- **SOCIAL SCIENCES:** EXAMINING RELATIONSHIPS BETWEEN POLITICAL AFFILIATION AND SOCIAL ISSUES, OR BETWEEN

EDUCATIONAL ATTAINMENT AND EMPLOYMENT STATUS.

- **QUALITY CONTROL:** DETERMINING IF DEFECTS IN MANUFACTURED PRODUCTS ARE EVENLY DISTRIBUTED OR IF THEY TEND TO OCCUR IN CLUSTERS.
- **PSYCHOLOGY:** ASSESSING IF RESPONSES TO SURVEY QUESTIONS ARE INDEPENDENT OF EXPERIMENTAL CONDITIONS.

LIMITATIONS OF THE CHI SQUARED TEST

WHILE POWERFUL, THE CHI-SQUARED TEST HAS LIMITATIONS THAT USERS SHOULD BE AWARE OF:

- **ONLY FOR CATEGORICAL DATA:** IT CANNOT BE USED DIRECTLY WITH CONTINUOUS OR INTERVAL DATA.
- **SENSITIVE TO SAMPLE SIZE:** WITH VERY LARGE SAMPLE SIZES, EVEN TINY, PRACTICALLY INSIGNIFICANT DIFFERENCES CAN BECOME STATISTICALLY SIGNIFICANT, LEADING TO POTENTIAL MISINTERPRETATION OF REAL-WORLD IMPORTANCE. CONVERSELY, SMALL SAMPLE SIZES MAY LACK THE POWER TO DETECT REAL ASSOCIATIONS.
- **DOES NOT MEASURE STRENGTH OF ASSOCIATION:** A SIGNIFICANT CHI-SQUARED VALUE INDICATES AN ASSOCIATION EXISTS BUT DOESN'T QUANTIFY ITS STRENGTH OR DIRECTION. MEASURES LIKE CRAMER'S V OR ODDS RATIOS ARE NEEDED FOR THIS.
- **ASSUMPTION OF INDEPENDENCE:** VIOLATIONS OF THE INDEPENDENCE ASSUMPTION (E.G., REPEATED MEASURES ON THE SAME INDIVIDUALS WITHOUT ACCOUNTING FOR IT) CAN INVALIDATE THE RESULTS.
- **ASSUMPTION OF EXPECTED FREQUENCIES:** SMALL EXPECTED CELL FREQUENCIES CAN LEAD TO INACCURATE RESULTS.
- **CAUSATION VS. ASSOCIATION:** A SIGNIFICANT CHI-SQUARED TEST INDICATES AN ASSOCIATION, BUT IT DOES NOT IMPLY CAUSATION. CORRELATION DOES NOT EQUAL CAUSATION.

FREQUENTLY ASKED QUESTIONS

Q: WHAT IS THE MAIN PURPOSE OF PERFORMING A CHI SQUARED TEST?

A: THE MAIN PURPOSE OF A CHI SQUARED TEST IS TO DETERMINE IF THERE IS A STATISTICALLY SIGNIFICANT ASSOCIATION BETWEEN TWO CATEGORICAL VARIABLES OR IF AN OBSERVED FREQUENCY DISTRIBUTION DIFFERS SIGNIFICANTLY FROM AN EXPECTED DISTRIBUTION.

Q: CAN A CHI SQUARED TEST BE USED FOR CONTINUOUS DATA?

A: NO, A CHI SQUARED TEST IS STRICTLY FOR CATEGORICAL DATA. IF YOU HAVE CONTINUOUS DATA, YOU WOULD TYPICALLY NEED TO CATEGORIZE IT FIRST (E.G., BY CREATING BINS OR INTERVALS) OR USE DIFFERENT STATISTICAL TESTS DESIGNED FOR CONTINUOUS VARIABLES.

Q: WHAT IS THE DIFFERENCE BETWEEN THE CHI SQUARED TEST FOR INDEPENDENCE AND THE CHI SQUARED TEST FOR HOMOGENEITY?

A: THE CHI SQUARED TEST FOR INDEPENDENCE EXAMINES IF THERE IS AN ASSOCIATION BETWEEN TWO CATEGORICAL VARIABLES WITHIN A SINGLE POPULATION. THE CHI SQUARED TEST FOR HOMOGENEITY COMPARES THE DISTRIBUTION OF A CATEGORICAL

VARIABLE ACROSS TWO OR MORE DISTINCT POPULATIONS TO SEE IF THE PROPORTIONS ARE THE SAME.

Q: WHAT DOES IT MEAN IF MY P-VALUE IS LESS THAN 0.05 IN A CHI SQUARED TEST?

A: IF YOUR P-VALUE IS LESS THAN 0.05 (OR YOUR CHOSEN SIGNIFICANCE LEVEL), YOU REJECT THE NULL HYPOTHESIS. THIS INDICATES THAT THE OBSERVED DIFFERENCES OR ASSOCIATIONS IN YOUR DATA ARE STATISTICALLY SIGNIFICANT AND UNLIKELY TO BE DUE TO RANDOM CHANCE.

Q: WHAT HAPPENS IF MY EXPECTED CELL FREQUENCIES ARE TOO SMALL FOR A CHI SQUARED TEST?

A: IF YOUR EXPECTED CELL FREQUENCIES ARE TOO SMALL (E.G., BELOW 5 IN MANY CELLS), THE CHI SQUARED APPROXIMATION MAY NOT BE ACCURATE. FOR 2x2 TABLES, FISHER'S EXACT TEST IS A COMMON ALTERNATIVE. FOR LARGER TABLES, YOU MIGHT CONSIDER COMBINING CATEGORIES OR USING EXACT TEST METHODS IF AVAILABLE IN YOUR SOFTWARE.

Q: DOES A SIGNIFICANT CHI SQUARED RESULT MEAN ONE VARIABLE CAUSES THE OTHER?

A: NO, A SIGNIFICANT CHI SQUARED TEST ONLY INDICATES AN ASSOCIATION BETWEEN VARIABLES. IT DOES NOT IMPLY CAUSATION. MANY OTHER FACTORS COULD BE INVOLVED, AND FURTHER RESEARCH OR EXPERIMENTAL DESIGN IS NEEDED TO ESTABLISH CAUSALITY.

Q: HOW ARE DEGREES OF FREEDOM CALCULATED FOR A CHI SQUARED TEST?

A: FOR A GOODNESS-OF-FIT TEST WITH 'K' CATEGORIES, $DF = k - 1$. FOR A TEST OF INDEPENDENCE OR HOMOGENEITY IN AN 'R' X 'C' CONTINGENCY TABLE, $DF = (R - 1) \times (C - 1)$.

Q: WHAT ARE SOME COMMON MISTAKES TO AVOID WHEN PERFORMING A CHI SQUARED TEST?

A: COMMON MISTAKES INCLUDE USING THE TEST WITH CONTINUOUS DATA, VIOLATING THE INDEPENDENCE OF OBSERVATIONS ASSUMPTION, HAVING TOO MANY SMALL EXPECTED CELL FREQUENCIES WITHOUT APPROPRIATE ADJUSTMENTS, AND MISINTERPRETING A SIGNIFICANT RESULT AS EVIDENCE OF CAUSATION.

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